

Fair Coexistence of Scheduled and Random Access Wireless Networks: Unlicensed LTE/WiFi

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Abstract—We study the fair coexistence of scheduled and random access transmitters sharing the same frequency channel. Interest in coexistence is topical due to the need for emerging unlicensed LTE technologies to coexist fairly with WiFi. However, this interest is not confined to LTE/WiFi as coexistence is likely to become increasingly commonplace in IoT networks and beyond 5G. In this paper, we show that mixing scheduled and random access incurs an inherent throughput/delay cost and the cost of heterogeneity. We derive the joint proportional fair rate allocation, which casts useful light on current LTE/WiFi discussions. We present experimental results on inter-technology detection and consider the impact of imperfect carrier sensing.

Index Terms—Coexistence, spectrum sharing, unlicensed LTE, LTE-U, LAA-LTE, WiFi, CSAT, LBT, LBE, proportional fairness.

I. INTRODUCTION

IN THIS paper we study fair time-based sharing of scheduled and random access transmitters coexisting in the same channel. Scheduled approaches transmit at regular instants of time (*slot/frame/subframe* boundaries) whereas random access methods use carrier sensing to divide time up into variable-size slots. We focus on the resulting MAC layer interactions and on joint MAC design for coexistence. Our main contributions are the following: (i) we show that mixing scheduled and random access incurs an inherent throughput/delay cost, which we refer to as the cost of heterogeneity, (ii) we develop a joint throughput model for scheduled and random access transmitters sharing the same band, (iii) we derive the joint proportional fair rate allocation and (iv) we present experimental measurements demonstrating the impact of imperfect carrier sensing by random access transmitters and show that our analytic results can be extended to encompass this.

While fair coexistence of scheduled and random access transmitters is of fundamental interest, it is particularly topical

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due to the current interest in operating LTE in unlicensed bands where WiFi is already widely deployed. Regulators require mobile cellular operators to show that LTE, which is a scheduled protocol, can coexist in a *fair* way with existing WiFi networks, which use random access [1]. In this context traditional power control solutions are of limited use and the requirement is to take into account the MAC layer interactions between the scheduled and random access approaches.

Two main LTE mechanisms for coexistence with WiFi are presently under consideration. Namely, *Listen Before Talk with Load Based Equipment* (LBT/LBE) and *Carrier Sensing and Adaptive Transmission* (CSAT) [2], [3]. LBT/LBE uses carrier sensing and sends a reservation signal to grab the channel from WiFi. In contrast, CSAT schedules transmissions according to a specified duty-cycle, oblivious to the channel status when a transmission is scheduled to start. We will see that these two approaches are indeed two fundamental ways to ensure that a scheduled network has reasonable chances to transmit when sharing a channel with random access transmitters. Further, our results establish that these two approaches can be operated in a proportional fair manner and show how this can be achieved, thereby providing significant input into current discussions on their ability to ensure fair coexistence with WiFi.¹

We note that interest in fair coexistence is not confined to LTE/WiFi, but also includes coexistence of WiFi and the TDMA access of Zigbee [5] as well as WiFi and WiMaX [6]. It is also likely to be an important issue in the Internet of Things (IoT) context, where (i) Time-Slotted Channel Hopping (TSCH) protocols may be expected to coexist with random access approaches, both of which are defined in the IEEE 802.15.4e-2015 standard [7] and (ii) protocols such as the upcoming IEEE 802.11ah [8] will need to coexist with Low Power Wide Area (LPWA) networks such as SigFox and LoRa [9]. More generally, we expect this kind of heterogeneity to become increasingly commonplace in the 5G era and beyond given the expected opportunistic use of spectrum and the growing range of network access technologies.

II. RELATED WORK

Coexistence among different technologies has traditionally been studied from an interference point of view, especially when coexisting devices have very different capabilities such as in the case of coexistence among WiFi and

¹Note that we are not addressing whether heterogeneous scenarios can be more efficient than single-tech scenarios, as in e.g. [4], but how two heterogeneous technologies can fairly share the common wireless medium.

Bluetooth/Zigbee [10]. However, taking into consideration the interactions among heterogeneous channel access mechanisms, in particular between scheduled (TDMA-like) and random-access mechanisms, allows for new insight and more scope for ensuring fair coexistence. Previous work on coexistence of scheduled and random access mechanisms has considered WiFi and the TDMA access of Zigbee [5] plus WiFi and WiMaX [6], [11]. However, this work does not aim at providing formal fairness guarantees. Recently, coexistence of WiFi and LTE has started to attract considerable interest. The risks of employing legacy LTE in unlicensed bands without proper access control that ensures fair coexistence has been made quite evident in e.g. [12] (via simulations), [13] (via analysis) or [14] (via experiments). The 3GPP's study on LTE/WiFi coexistence [15] shows that the presence of unlicensed LTE networks may degrade the performance of existing 802.11 stations if coexistence protocols are not efficient. However, in this study the implementation details of the coexistence mechanisms used are not specified. Nokia, Qualcomm and Huawei have presented their own white papers on the topic [16]–[18] showing satisfactory results. However, once again, details of the implemented access mechanisms (LBT and CSAT) and simulation models used in these papers are not public. Fair coexistence of LBT has been studied in [19]–[21]. However, in these works the WiFi models used lack collisions and idle periods. Fairness has also been studied in [22] for a simplified version of the LBT scheme and without consideration of collisions between both technologies. Recently, [23] has studied how to jointly determine the channel selection, carrier aggregation and fractional spectrum access for CSAT. However, they do not consider the inherent heterogeneity cost and the resulting model complexity does not allow for explicit solution. The present paper substantially extends our initial findings in [24], being both more general and taking account of important aspects such as non-saturated stations and imperfect inter-technology signal detection.

III. IMPLICATIONS OF HETEROGENEITY

Our interest is in coexistence of scheduled and random access networks in the same frequency band. In this section we begin by considering the consequences for scheduled transmitters of being constrained to transmit at fixed slot times.

Throughout this article, if not otherwise specified, we make the following assumptions in our analysis and simulations: (i) no channel errors, (ii) all nodes are in mutual coverage range (no hidden terminals), (iii) all collisions result in data loss (no capture), (iv) saturation conditions (both the scheduled and the random access transmitters always have a packet to send). Additionally, we assume that: (i) the coexisting scheduled and random access networks use the same single channel and that (ii) there is only one scheduled transmitter, which may represent coordinated transmission from multiple scheduled users. Section VII provides a discussion on these assumptions and on how they can be relaxed.

A. Idle Channel Probability at Periodic Slot Boundaries

Intuitively, when the random access transmitters are making efficient use of the channel, so leaving only a small amount

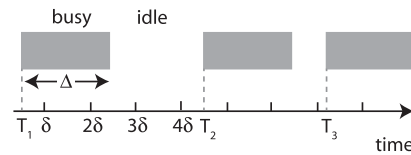


Fig. 1. Illustrating transmission slots with variable timing T_k (random access transmitter) and with fixed timing of period δ (scheduled transmitter).

of idle time, we expect that the probability of a scheduled transmitter finding the channel idle at the start of an admissible transmission slot will be small. We formalise this as follows.

Consider a set of transmitters A that are constrained to transmit in pre-defined time slots $[(j-1)\delta, j\delta)$, $j = 1, 2, \dots$ each of duration δ (scheduled transmitters). This might, for example, correspond to a network where the fixed time slots arise due to the use of a TDMA scheduler which divides time into slots and then schedules transmissions in these slots. Suppose now that these transmitters A share the radio channel with a set of transmitters B (random access transmitters) which transmit during intervals $[T_k, T_k + \Delta_k)$, $k = 1, 2, \dots$, with $T_{k+1} \geq T_k + \Delta_k$ and random variable Δ_k the duration of the k 'th transmission. The start times $\{T_k\}$ are random variables that need not be synchronised with start times $(j-1)\delta$ of the pre-defined time slots used by transmitters A . The setup is illustrated schematically in Fig. 1.

We begin by asking for what fraction of A slot start times $\{(j-1)\delta, j = 1, 2, \dots\}$ the channel is idle (i.e. there are no B transmissions in progress). This provides a measure of the transmission slots where the transmitters A can schedule transmissions without interfering with the transmitters B . Let $\mathcal{T} := \cup_{k=1,2,\dots} [T_k, T_k + \Delta_k)$ denote the aggregate time occupied by B transmissions and define random variable X_j that takes value 1 when $(j-1)\delta \in \mathcal{T}$ and 0 otherwise. We are interested in the value of $p_{\text{idle}} := \lim_{J \rightarrow \infty} \frac{1}{J} \sum_{j=1}^J (1 - X_j)$.

We can think of the A transmitters as periodically sampling the channel at times $\{(j-1)\delta\}$ and p_{idle} as the probability that the channel is idle when they sample it. Assuming that the start times and durations $\{(T_k, \Delta_k), k = 1, 2, \dots\}$ form a mixing process and that the sampling is not perturbing this process, then the NIMASTA property (a generalisation of PASTA, ‘‘Poisson Arrivals See Time Averages’’) holds [25, Th. 2] and p_{idle} is equal to the fraction of time the channel is idle i.e. $p_{\text{idle}} = \lim_{K \rightarrow \infty} \frac{\sum_{k=1}^{K-1} T_{k+1} - (T_k + \Delta_k)}{T_K}$.

1) *Example: CSMA/CA:* Suppose that the scheduled transmitters A are silent (we will relax this shortly) and the random access transmitters B consist of n stations using CSMA/CA. Letting $Z_{t,i}$ be a random variable which takes value 1 when CSMA/CA station i transmits in MAC slot t , we assume that the $\{Z_{t,i}, t = 1, 2, \dots\}$ are i.i.d. and let $\tau_i = \text{Prob}(Z_{t,i} = 1)$ denote the probability that station i transmits in a MAC slot. Then $p_s = \sum_{i=1}^n \tau_i \prod_{k=1, k \neq i}^n (1 - \tau_k)$ is the probability of a successful transmission and $p_c = 1 - p_s - p_e$, with $p_e = \prod_{i=1}^n (1 - \tau_i)$, is the probability of a collision between transmissions. Let T_b denote the duration of a successful transmission, including the MAC ACK, and T_{fra} the duration of a data frame without corresponding ACK i.e. of a

TABLE I
PARAMETERS IEEE 802.11ac [26]

Slot Duration (σ)	9 μ s
DIFS	34 μ s
SIFS	16 μ s
PLCP Preamble+Headers Duration (T_{plcp})	40 μ s
PLCP Service Field (L_s)	16 bits
MPDU Delimiter Field (L_{del})	32 bits
MAC Header ($L_{\text{mac-h}}$)	288 bits
Tail Bits (L_t)	6 bits
ACK Length (L_{ack})	256 bits
Payload (D)	12000 bits

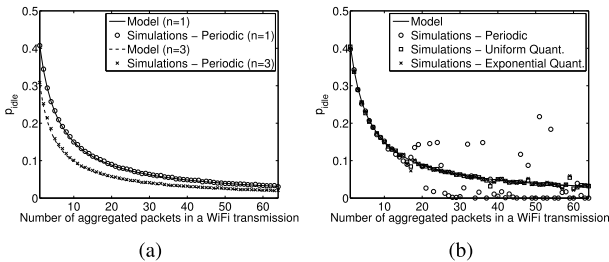


Fig. 2. Probability of observing an idle channel at slot boundaries of fixed period $\delta = 100$ ms in a channel occupied by an 802.11 WLAN with $n = 1$ and $n = 3$ WiFi stations. Simulation results are averages of 100 simulation runs with 50 s time horizon. (a) Without A transmissions. (b) With A transmissions ($n = 1$).

colliding transmission. Then the $\{\Delta_k, k = 1, 2, \dots\}$ are i.i.d. with $\Delta_k = T_b$ for successful transmissions and $\Delta_k = T_{\text{fra}}$ for collisions. Since the transmissions form a renewal process,

$$p_{\text{idle}} = 1 - \frac{p_s T_b + p_c T_{\text{fra}}}{\mathbb{E}[M]}, \quad (1)$$

where $\mathbb{E}[M]$ is the average MAC slot duration of CSMA.

To proceed we insert typical 802.11ac [26] values into (1). Namely,

$$T_{\text{fra}} = T_{\text{plcp}} + \left[\frac{L_s + n_{\text{agg}}(L_{\text{del}} + L_{\text{mac-h}} + D) + L_t}{n_{\text{sym}}} \right] T_s,$$

$$T_{\text{ack}} = T_{\text{plcp}} + \left[\frac{L_s + L_{\text{ack}} + L_t}{n_{\text{sym}}} \right] T_s, T_b$$

$$= T_{\text{fra}} + \text{SIFS} + T_{\text{ack}},$$

where n_{sym} is the number of bits per OFDM symbol, T_s is the symbol duration, n_{agg} is the number of packets aggregated in a transmission and the values of the various parameters are specified in Table I. We also set $\mathbb{E}[M] = \sigma p_e + (p_s + p_c)$ (DIFS + T_b), where σ is the duration of a PHY slot [27].

Fig. 2(a) shows p_{idle} calculated using (1) vs the number of packets aggregated in a transmission (effectively varying T_{fra}) for a WLAN with $n = 1$ and $n = 3$ stations and δ deterministic (referred as “Periodic”) and equal to 100 ms. The parameters used are detailed in Table I, $\tau_i, i = 1, \dots, n$ set to 1/16 and modulation and coding scheme configured to 64-QAM 5/6 with 20 MHz channel width. Also shown in Fig. 2(a) is the measured fraction of periodic slots $\{(j-1)\delta, j = 1, 2, \dots\}$ obtained by numerical simulation and, as expected, it can be seen that they are in good agreement.

It can be seen from Fig. 2(a) that the value of p_{idle} is relatively small (in general, $<50\%$ and below 5% for larger WLAN packet sizes), indicating that relatively few non-colliding transmission slots are available for use by the scheduled transmitters A .

B. Cost of Heterogeneity

An important consequence of the fact that p_{idle} is typically small is that for transmitters A , which are restricted to transmit at periodic times $\{(j-1)\delta, j = 1, 2, \dots\}$, at the great majority of the potential transmission times competing transmissions B are already in progress. This means that for the transmitters A to have a reasonable chance to transmit at the start of a slot boundary, they could either act: (i) *Preemptively*: transmitting at the start of a slot boundary regardless of the channel status, thus potentially causing collisions with transmitters B or (ii) *Opportunistically*: grabbing the channel when empty and transmitting a reservation signal until the next slot boundary (assuming the transmitters B can effectively detect A 's transmissions,² then a reservation signal will make transmitters B refrain from accessing the channel). Note that the *Preemptive* approach can be identified with the LTE CSAT approach and the *Opportunistic* approach with LBT/LBE. Both cases incur a reduction of effective airtime since in (i) additional collisions are generated, and so network throughput is lowered, while in (ii) the reservation signal reduces the airtime available for data transmissions which again lowers network throughput.³ That is, the heterogeneity of the transmission slots used by transmitters A and B necessarily incurs an overhead.

We quantify this overhead in more detail later since it is technology-dependent, but for now we note that provided transmitters B can effectively detect transmitters A (e.g. via carrier sensing), the throughput overhead can be reduced by increasing the duration of the transmissions by scheduled stations A . This can be seen by noting that the overhead is then a per-transmission one (either a single collision or a single reservation signal is incurred per transmission). Hence, increasing the duration of A transmissions amortises this overhead over a larger amount of data and increases network throughput efficiency. However, increasing the duration of A transmissions will tend to increase the delay experienced by the B transmissions since these now need to wait longer for A transmissions to finish before they can start to transmit. The overhead incurred by use of heterogeneous transmission slots can therefore be expressed as a throughput/delay trade-off.

In summary, heterogeneity incurs a per-transmission overhead which can be alleviated by increasing the duration of the scheduled transmissions provided that random access transmitters effectively detect those. In turn, that solution tends to increase the delay of the random transmissions.

C. Example Revisited: Random Scheduled Starting Times

Recall that in the previous example we assumed that the scheduled transmitters A are silent. We now relax

²We will revisit this assumption later in Section VI.

³Note that in contrast to the airtime loss due to collisions, the reservation signal could be used to transmit control or other information.

this assumption. The most difficult case is when scheduled transmissions A can be detected by the random access transmitters B , e.g. via carrier sensing, and so the random access transmissions are coupled to the scheduled transmissions. In this case the NIMASTA property does not hold. Nevertheless, we show below that provided the time between scheduled transmissions is suitably randomised then simulations indicate that the insight from the previous analysis generally remains valid.

We begin by highlighting the impact of coupling between the random access and scheduled transmissions via carrier sensing. Fig. 2(b) shows measurements of p_{idle} obtained by numerical simulation for a setup similar to that in Section III-A.1 and can be directly compared with Fig. 2(a). The difference is that now there is an A transmitter which starts transmitting at a slot boundary regardless of the channel status and keeps transmitting for a fixed duration $T_{\text{on}} = 50$ ms which is a multiple of the slot duration $\delta = 1$ ms. It then remains silent for a period T_{off} seconds.

When T_{off} is deterministic and fixed at $T_{\text{off}} = 50$ ms (labelled ‘‘Periodic’’ in Fig. 2(b)), it can be seen that p_{idle} exhibits quite complex behaviour as the duration of the WLAN transmissions is varied. Further inspection confirms that this is associated with interactions between the A and B transmissions induced by detection of A transmissions by the B nodes. Namely, due to carrier sensing B transmissions are deferred during each T_{on} interval and then restart during the T_{off} interval. The B transmission behaviour following restart is constrained (there can be no ongoing B transmissions at the start of a T_{off} interval) and this leads to quantisation effects related to the number of complete B transmissions that can be fitted into the T_{off} interval. Observe that this quantisation effect is non-negligible even when T_{off} is relatively long (T_{off} is set to 50 ms in Fig. 2(b)).

For comparison, Fig. 2(b) shows the corresponding data when T_{off} is drawn randomly after each T_{on} interval according to uniform and exponential distributions with mean 50 ms, minimum 10 ms and rounded to a multiple of δ (labelled as ‘‘Uniform Quant.’’ and ‘‘Exponential Quant.’’, respectively). It can be seen that randomising T_{off} largely removes the quantisation effects and the measured p_{idle} is once again in good agreement with (1). The analysis here indicates that it is probably preferable to randomise the duration of the T_{off} intervals to avoid quantisation effects and thus, make results less sensitive to small changes in the input parameters.

IV. FAIR COEXISTENCE

In this section we consider fairness for both of the fundamental coexistence approaches noted in the previous section (*Preemptive* and *Opportunistic*), taking a proportional fair approach. Since achieving fair coexistence is only of concern when we want to make intensive use of the network resources, we consider in the following carrier sense random access, as mechanisms without carrier sense are well known to perform poorly in these conditions, e.g., [28].

A. Throughput Model

We begin by developing a throughput model when transmitters A and B share the same wireless channel. We consider

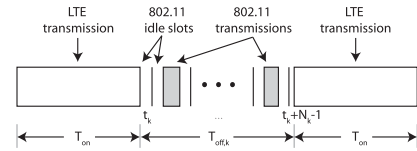


Fig. 3. Schematic showing scheduled/random access transmission timing.

the coexistence approaches in a unified fashion, to simplify presentation of both the model and the fairness analysis.

We consider a single scheduled transmitter (A) sharing the network with a set of n transmitters B . Let S_k , $k = 1, 2, \dots$ denote the times when scheduled transmissions start. Each scheduled transmission is of duration T_{on} , so the silent/off interval between scheduled transmissions k and $k + 1$ is of duration $T_{\text{off},k} := S_{k+1} - S_k - T_{\text{on}}$, see Fig. 3. From the insights obtained in Section III, we assume that random variables $T_{\text{off},k}$, $k = 1, 2, \dots$ are i.i.d. with mean $\bar{T}_{\text{off}} := \mathbb{E}[T_{\text{off}}]$. As we pointed out before, we also assume that transmitters B use CSMA/CA. We further consider that transmitters B are able to detect the channel as being busy during a scheduled transmission with no error; so no CSMA/CA station starts transmission during a T_{on} period, we will revisit this assumption later in Section VI. Note that there may be a collision at the start of a T_{on} period when transmitter A starts transmitting while a CSMA/CA transmission is already in progress.

1) *CSMA/CA MAC Slots*: During the $T_{\text{off},k}$ period when transmitter A is silent following the end of a T_{on} period, the random access stations perform their usual CSMA/CA mechanism. This process partitions time into MAC slots which may be either an idle slot, of duration σ , or a busy slot, of average duration Δ . We assume that the average duration of a successful transmission is equal to the average duration of a collision.⁴ We index these MAC slots during the $T_{\text{off},k}$ period by $t_k, t_k + 1, \dots, t_k + N_k - 1$, where the number of MAC slots $N_k := t_{k+1} - t_k$ in the $T_{\text{off},k}$ period is a random variable, see Fig. 3. Note that at the end of the $T_{\text{off},k}$ period there will generally be a partial MAC slot, since the end of the $T_{\text{off},k}$ period need *not* be aligned with the CSMA/CA MAC slot boundaries, but $t_k + N_k$ indexes the last full MAC slot.

2) *CSMA/CA Events*: Let $Z_{t,j}$ be a random variable which takes the value 1 when a CSMA/CA station j transmits in MAC slot t . We assume that the $Z_{t,j}$, $t = 1, 2, \dots$ are i.i.d., $Z_{t,j} \sim Z_j$ and let $\tau_j := \Pr(Z_j = 1)$. We also assume that the $Z_{t,j}$, $j = 1, \dots, n$ are independent.

Let X_t be a random variable which takes the value 1 when MAC slot t is busy ($Z_{t,j} = 1$ for at least one $j \in \{1, \dots, n\}$), and 0 otherwise. The X_t , $t = 1, 2, \dots$ are i.i.d., $X_t \sim X$, with $p_e := \Pr(X = 0) = \prod_{i=1}^n (1 - \tau_i)$. Since the X_t , $t = 1, 2, \dots$ are i.i.d. and the $T_{\text{off},k}$, $k = 1, 2, \dots$ are also i.i.d. the number N_k of MAC slots in the $T_{\text{off},k}$ periods $k = 1, 2, \dots$ are i.i.d., $N_k \sim N$. The duration of MAC slot t is $M_t := \sigma + X_t (\Delta_t - \sigma)$, with Δ_t the specific duration of the busy slot t . The M_t , $t = 1, 2, \dots$ are i.i.d., $M_t \sim M$ with $\mathbb{E}[M] = \sigma p_e + \Delta(1 - p_e)$.

Let $Y_{t,j}$ be a random variable which takes the value 1 when there is a successful (non-colliding) transmission by a

⁴For a discussion on this assumption refer to Section VII.

CSMA/CA station j in MAC slot t , and 0 otherwise. The $Y_{t,j}$, $t = 1, 2, \dots$ are i.i.d., $Y_{t,j} \sim Y_j$, with $p_{succ,j} := \Pr(Y_j = 1) = \frac{\tau_j}{1-\tau_j} p_e$. The number of successful transmissions in the $T_{off,k}$ period is $W_{k,j} := \sum_{t=t_k}^{t_k+N_k-1} Y_{t,j}$ and the mean rate in bit/s of a CSMA/CA station j is $s_{csma,j} := \lim_{K \rightarrow \infty} \frac{\sum_{k=1}^K W_{k,j}}{\sum_{k=1}^K T_{on} + T_{off,k}} D_j$, where D_j is the number of data bits communicated by station j in a successful transmission.

3) *CSMA/CA Throughput*: The $W_{k,j}$, $k = 1, 2, \dots$ are i.i.d., $W_{k,j} \sim W_j$, and the $T_{off,k}$, $k = 1, 2, \dots$ are also i.i.d., $T_{off,k} \sim T_{off}$ (but note that $W_{k,j}$ and $T_{off,k}$ are not independent since the number of successful transmissions depends on the duration of the k 'th *off* period). The $W_{k,j}$, $T_{off,k}$, $k = 1, 2, \dots$ define a renewal-reward process and it follows that $s_{csma,j} = \frac{\mathbb{E}[W_j]}{T_{on} + \mathbb{E}[T_{off}]} D_j$. We have that $\mathbb{E}[W_j] = \mathbb{E}[Y_j] \mathbb{E}[N]$, assuming Y_j and N are independent, which holds for large N , and $\mathbb{E}[Y_j] = p_{succ,j}$. It remains to determine $\mathbb{E}[N]$ (the average number of full CSMA/CA MAC slots in an *off* period of transmitter A).

Let $\hat{T}_{off,k} = \sum_{t=t_k}^{t_k+N_k-1} M_t$. That is, $\hat{T}_{off,k} \leq T_{off,k}$ is the duration of that part of the $T_{off,k}$ period occupied by full CSMA/CA MAC slots *i.e.* excluding any partial MAC slot at the end of the period that may take place when transmitter A uses the *Preemptive* approach. It follows that $\mathbb{E}[N] = \frac{\mathbb{E}[\hat{T}_{off}]}{\mathbb{E}[M]}$ since the M is independent of N , again considering N sufficiently large. Hence,

$$s_{csma,j} = \frac{p_{succ,j}}{\sigma p_e + \Delta(1-p_e)} \frac{\mathbb{E}[\hat{T}_{off}]}{T_{on} + \bar{T}_{off}} D_j. \quad (2)$$

Observe that $s_j := \frac{p_{succ,j}}{\sigma p_e + \Delta(1-p_e)} D_j$ is just the usual expression for the throughput of a CSMA/CA station (as in [27] for the case of 802.11), but that this is now scaled by $\frac{\mathbb{E}[\hat{T}_{off}]}{T_{on} + \bar{T}_{off}}$.

4) $\mathbb{E}[\hat{T}_{off}]$: To complete the expression for CSMA/CA throughput we require $\mathbb{E}[\hat{T}_{off}]$. We show in the following how to compute this for the two mechanisms considered.

Preemptive approach: Since in the *Preemptive* approach, transmitter A transmits regardless of the channel status, a scheduled transmission may start part way through a CSMA/CA MAC slot. In this case we might approximate $\mathbb{E}[\hat{T}_{off}]$ by $\mathbb{E}[T_{off}]$, and we can expect this approximation to be accurate when $\mathbb{E}[T_{off}]$ is sufficiently larger than a CSMA/CA MAC slot (M_t) as the effect of any partial MAC slot on the total off duration becomes negligible. However, when $\mathbb{E}[T_{off}]$ is smaller it is necessary to use a more accurate approximation for $\mathbb{E}[\hat{T}_{off}]$. We adopt the following. When the start times S_k , $k = 1, 2, \dots$ of the scheduled transmissions satisfy the lack of anticipation property, *e.g.* when the spacing $S_{k+1} - S_k$ is drawn from an exponential distribution [25], then the transmissions from transmitter A satisfy the PASTA property. This is in turn in line with the insights obtained in Section III-C. Then, the probability that the start of a transmission from transmitter A coincides with a CSMA/CA transmission is $p_{txA} = \frac{(1-p_e)\Delta}{\mathbb{E}[M]}$. Assuming that on average the start of an *on* period that collides with a CSMA/CA transmission occurs half-way through the

CSMA/CA transmission, then

$$\begin{aligned} \mathbb{E}[\hat{T}_{off}] &= \mathbb{E}[T_{off}](1 - p_{txA}) + (\mathbb{E}[T_{off}] - \Delta/2)p_{txA} \\ &= \bar{T}_{off} - c_1, \end{aligned} \quad (3)$$

c_1 is the average airtime lost due to a partial CSMA/CA MAC slot before the start of an *on* period (when the scheduled transmitter starts transmitting) with $c_1 = (\Delta/2)p_{txA}$.

Opportunistic approach: In the *Opportunistic* approach, we assume that the start of an *on* period is aligned with a CSMA/CA MAC slot boundary since the scheduled network must in this case detect CSMA/CA transmissions and can then ensure this. Therefore there are no partial MAC slots and

$$\mathbb{E}[\hat{T}_{off}] = \bar{T}_{off}. \quad (4)$$

Equivalently, $\mathbb{E}[\hat{T}_{off}] = \bar{T}_{off} - c_1$ where the average airtime lost due to a partial CSMA/CA MAC slot before the start of an *on* period is now $c_1 := 0$. Also, the probability that the start of an *on* period coincides with a CSMA/CA transmission is just $p_{txA} = 1 - p_e$, that is, the probability of having at least one CSMA/CA station transmitting in a given MAC slot.

5) *Scheduled Network Throughput*: Let r denote the transmit rate in bits/s of transmitter A . When the start time of an *on* period does not coincide with a CSMA/CA transmission then the error-free transmission of transmitter A is of duration T_{on} *i.e.* rT_{on} bits are transmitted. When the *on* start time coincides with a CSMA/CA transmission then we assume that the first fully or partially overlapping slots of the transmission are lost. The precise behaviour differs for the *Preemptive* and *Opportunistic* approaches, as follows.

Preemptive approach: On average the start of a transmission from transmitter A that collides with a CSMA/CA transmission occurs half-way through the CSMA/CA transmission, and so on average the first $\Delta/2$ seconds of the transmission from the scheduled network are lost. Assuming that partial overlap of a scheduled slot with a CSMA/CA transmission leads to loss of the whole slot, then $r(T_{on} - \lceil \frac{\Delta}{2\delta} \rceil \delta)$ bits are transmitted by transmitter A , where δ denotes the duration of a pre-defined slot in the scheduled network. It follows that the resulting throughput when using the *Preemptive* approach is:

$$\begin{aligned} s_{txA} &= r \frac{T_{on}(1 - p_{txA}) + (T_{on} - \lceil \frac{\Delta}{2\delta} \rceil \delta)p_{txA}}{T_{on} + \bar{T}_{off}} \\ &= r \frac{T_{on} - c_2}{T_{on} + \bar{T}_{off}}, \end{aligned} \quad (5)$$

where c_2 is the mean scheduled airtime during which collisions with the CSMA/CA transmitters occur, with $c_2 = \lceil \frac{\Delta}{2\delta} \rceil \delta p_{txA}$.

Opportunistic approach: Since in this case the scheduled transmissions are aligned with CSMA/CA MAC slots the duration of a collision between both networks is simply Δ . Additionally, since the transmitter A has to transmit a reservation signal until the next subframe boundary of average duration $T_{res} = \delta/2$, useful data transmission only occurs during $T_{on} - T_{res}$ and the number of bits transmitted at each *on* period when it suffers from a collision with the CSMA/CA network is: $r(T_{on} - \max(T_{res}, \lceil \frac{\Delta}{\delta} \rceil \delta))$. It follows that the throughput achieved by the scheduled network when using

the *Opportunistic* approach is:

$$s_{\text{txA}} = r \frac{T_{\text{on}} - c_2}{T_{\text{on}} + \bar{T}_{\text{off}}}, \quad (6)$$

where now $c_2 = \max(T_{\text{res}}, \lceil \frac{\Delta}{\delta} \rceil \delta) p_{\text{txA}} + T_{\text{res}}(1 - p_{\text{txA}})$ is the mean scheduled airtime during which collisions between scheduled and CSMA/CA transmissions occur and/or the scheduled transmitter sends a reservation signal.

B. Proportional Fair Allocation

We now derive the proportional fair channel time allocation when transmitter *A* (scheduled) and the n nodes of type *B* (CSMA/CA) share a channel and transmitter *A* uses either the: (i) *Preemptive* or (ii) *Opportunistic* approach.

Theorem 1 (Proportional Fair Rate Allocation): The proportional fair rate allocation assigns the following fraction of channel airtime to full CSMA/CA MAC slots:

$$\frac{\bar{T}_{\text{off}}^* - c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \frac{n}{n+1} \quad (7)$$

and the following fraction of airtime to the scheduled network:

$$\frac{T_{\text{on}} + c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = 1 - \frac{\bar{T}_{\text{off}}^* - c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \frac{1}{n+1}, \quad (8)$$

where \bar{T}_{off}^* is the proportional fair mean off time between scheduled transmissions, c_1 is the average airtime lost due to a partial CSMA/CA MAC slot before the start of an on period (when the scheduled transmitter starts transmitting).

Proof: Let $z = \bar{T}_{\text{off}}^* - c_1$, $\tilde{z} := \log z$, $\tilde{s}_{\text{csma},j} := \log s_{\text{csma},j}$ and $\tilde{s}_{\text{txA}} := \log s_{\text{txA}}$. Then,

$$\tilde{s}_{\text{csma},j} = \log s_j \frac{\bar{T}_{\text{off}}^* - c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \log s_j + \tilde{z} - \log(T_{\text{on}} + c_1 + e^{\tilde{z}}),$$

and

$$\begin{aligned} \tilde{s}_{\text{txA}} &= \log r \frac{T_{\text{on}} - c_2}{T_{\text{on}} + \bar{T}_{\text{off}}^*} \\ &= \log(r(T_{\text{on}} - c_2)) - \log(T_{\text{on}} + c_1 + e^{\tilde{z}}). \end{aligned}$$

It can be verified (by inspection of the second derivative) that $\log(T_{\text{on}} + c_1 + e^{\tilde{z}})$ is convex in \tilde{z} when $T_{\text{on}} + c_1 \geq 0$. Hence, putting the network constraints in standard form,

$$\tilde{s}_{\text{csma},j} - \log s_j - \tilde{z} + \log(T_{\text{on}} + c_1 + e^{\tilde{z}}) \leq 0, \quad j = 1, \dots, n \quad (9)$$

$$\tilde{s}_{\text{txA}} - \log q + \log(T_{\text{on}} + c_1 + e^{\tilde{z}}) \leq 0, \quad (10)$$

where $q := r(T_{\text{on}} - c_2)$, it can be seen that they are convex in decision variables $\tilde{s}_{\text{csma},j}$, \tilde{s}_{txA} and \tilde{z} .

The proportional fair rate allocation for the scheduled network is the solution to the following utility optimisation,

$$\begin{aligned} \max_{\tilde{s}_{\text{csma},j}, \tilde{s}_{\text{txA}}, \tilde{z}} \quad & \tilde{s}_{\text{txA}} + \sum_{j=1}^n \tilde{s}_{\text{csma},j} \\ \text{s.t.} \quad & \tilde{s}_{\text{csma},j} - \log s_j - \tilde{z} + \log(T_{\text{on}} + c_1 + e^{\tilde{z}}) \leq 0, \\ & j = 1, \dots, n \\ & \tilde{s}_{\text{txA}} - \log q + \log(T_{\text{on}} + c_1 + e^{\tilde{z}}) \leq 0. \end{aligned}$$

The optimisation is convex and satisfies the Slater condition, hence strong duality holds. The Lagrangian is,

$$\begin{aligned} L &= -\tilde{s}_{\text{txA}} - \sum_{j=1}^n \tilde{s}_{\text{csma},j} \\ &+ \theta(\tilde{s}_{\text{txA}} - \log q + \log(T_{\text{on}} + c_1 + e^{\tilde{z}})) \\ &+ \sum_{j=1}^n \lambda_j(\tilde{s}_{\text{csma},j} - \log s_j - \tilde{z} + \log(T_{\text{on}} + c_1 + e^{\tilde{z}})). \end{aligned}$$

The main KKT conditions are

$$-1 + \theta = 0, \quad -1 + \lambda_j = 0 \quad j = 1, \dots, n$$

$$\left(\theta + \sum_{j=1}^n \lambda_j\right) \frac{e^{\tilde{z}}}{T_{\text{on}} + c_1 + e^{\tilde{z}}} - \sum_{j=1}^n \lambda_j = 0.$$

Thus, at an optimum $\theta = 1$, $\lambda_j = 1$, $j = 1, \dots, n$ and

$$\frac{e^{\tilde{z}}}{T_{\text{on}} + c_1 + e^{\tilde{z}}} = \frac{n}{n+1}. \quad (11)$$

It can be verified (by inspection of the first derivative) that the LHS is monotonically increasing in \tilde{z} and so a unique solution \tilde{z} exists satisfying (11). Letting \tilde{z}^* denote this solution, the proportional fair \bar{T}_{off} value is given by $\bar{T}_{\text{off}}^* = e^{\tilde{z}^*} + c_1$. The channel time fraction available for full CSMA/CA MAC slots is

$$\frac{\bar{T}_{\text{off}}^* - c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \frac{e^{\tilde{z}^*}}{T_{\text{on}} + c_1 + e^{\tilde{z}^*}} = \frac{n}{n+1} \quad (12)$$

and the channel time fraction used by the scheduled network is

$$1 - \frac{\bar{T}_{\text{off}}^* - c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \frac{T_{\text{on}} + c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \frac{1}{n+1}. \quad (13)$$

C. Discussion

The scheduled transmission time T_{on} includes the reservation signal and/or the airtime due to collisions between scheduled and CSMA/CA transmitters. Hence, $T_{\text{on}} + c_1$ is the time spent transmitting plus the time spent on collisions, reservation signals and partial CSMA/CA MAC slots. Letting $(\bar{T}_{\text{off}}^* - c_1)/n$ denote the airtime *allocated* to a CSMA/CA station, including idle time and collisions with other CSMA/CA nodes, then Theorem 1 tells us that the proportional fair rate allocation equalises this airtime and $T_{\text{on}} + c_1$.

That is, the airtime allocated to the scheduled network is the same as the total channel time effectively used by the CSMA/CA network divided among the number of CSMA/CA transmitters. This seems quite intuitive and is similar to previous proportional fair analysis for WiFi-only settings [27], [29]; the most interesting point here is that the proportional fair allocation assigns the cost of heterogeneity, i.e., the airtime cost of a collision between transmitter *A* and the CSMA/CA network and of any reservation signals, to the scheduled network. On the other hand, the inefficiency of the random access mechanism (idle periods and collisions among CSMA/CA nodes) is accounted for in the total effective channel time of the CSMA/CA network. Note that one immediate consequence of the cost of heterogeneity being accounted for in the airtime

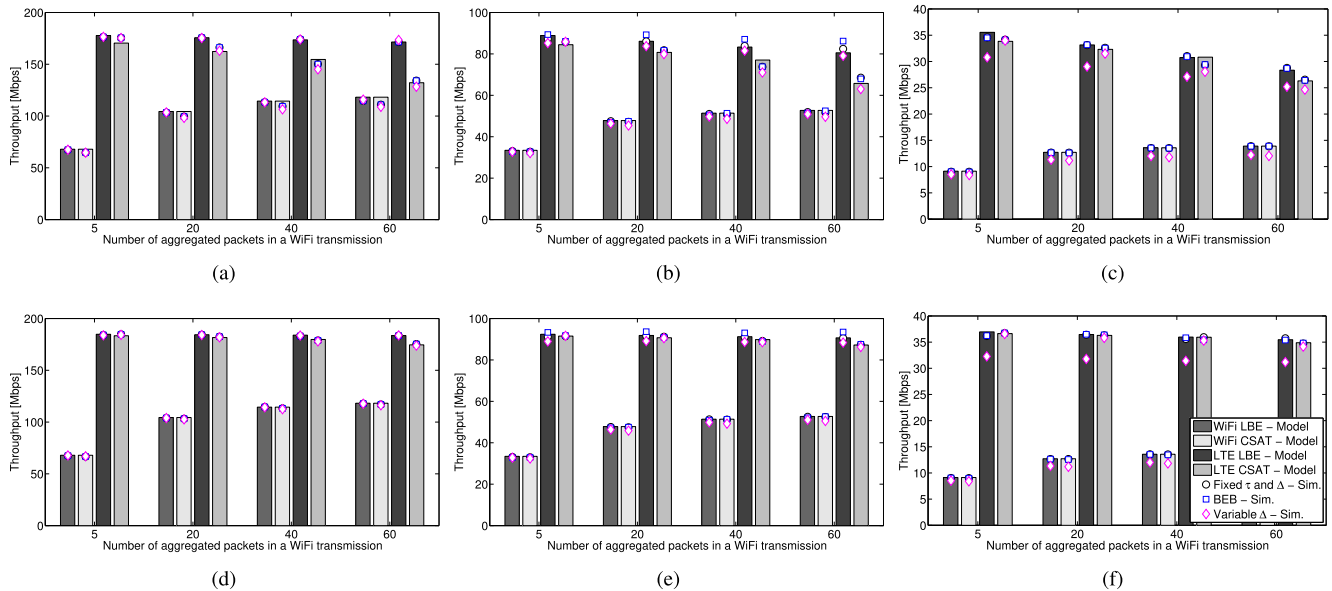


Fig. 4. Proportional fair throughput allocation for different configurations of n and T_{on} while varying n_{agg} (effectively changing the packet size of WiFi transmissions). Simulation results are averages of 100 simulation runs with 50 s time horizon. (a) $n = 1, T_{\text{on}} = 10$ ms. (b) $n = 3, T_{\text{on}} = 10$ ms. (c) $n = 9, T_{\text{on}} = 10$ ms. (d) $n = 1, T_{\text{on}} = 50$ ms. (e) $n = 3, T_{\text{on}} = 50$ ms. (f) $n = 9, T_{\text{on}} = 50$ ms.

allocated to the scheduled network is that both the *Preemptive* and *Opportunistic* approaches, when configured for a proportional fair rate allocation, result in the same throughput for the CSMA/CA network. Note as well that the fair rate allocation can be realised by appropriate operation of the scheduled transmitter and that no adaptation is needed by the CSMA/CA network. For more details refer to Section VII.

D. Example: Unlicensed LTE and 802.11

We revisit here the example in Section III-A.1 to illustrate the proportional fair allocation. As noted before, the *Preemptive* approach can be identified with the LTE CSAT approach and the *Opportunistic* approach with LBT/LBE. We use the same MAC parameters as in Section III-A.1. Additionally, for the LTE network throughput calculation we assume that the Control Format Indicator (CFI) is equal to 0 (i.e. we assume that the control information is sent through the licensed interface, which is in line with current 3GPP and LTE-U Forum discussions). To obtain the proportional fair allocation our throughput model is applied with $\mathbb{E}[M] = \sigma p_e + (T_b + \text{DIFS})(1 - p_e)$ and in the *Preemptive* case $p_{\text{txA}} = \frac{p_s T_b + p_c T_{\text{tra}}}{\mathbb{E}[M]}$. This accounts for the interframe spaces defined in 802.11 as well as for Δ now being different in the case of a successful transmission versus a collision.

1) *Cost of Heterogeneity*: Fig. 4 shows the WiFi and LTE proportional fair throughputs when using CSAT and LBE. Results are shown both for packet-level simulations⁵ and for the throughput model presented in Section IV-A. Simulations follow the specific channel access mechanisms with assumptions as listed in Section III and “Uniform Quant.” T_{off} (from Section III), including fixed τ and equal successful and collision durations (by fixing Δ_t). Since we assume fixed

802.11 transmission probability and packet sizes, we have also simulated the Binary Exponential Backoff (BEB) and variable WiFi packet sizes (with expectation matching the constant values used in the analysis) to assess the sensitivity of results to these considerations.⁶ Fig. 4 shows the impact of varying T_{on} , n and the number of aggregated packets in a WiFi transmission n_{agg} (effectively changing the packet size).

Observe that agreement between the analysis and simulations is generally accurate for fixed τ and Δ . However, we can observe small discrepancies for: (i) short T_{off} (in the case of WiFi throughput and CSAT) - Fig. 4a; and (ii) short T_{on} (in the case of LTE throughput and LBE and CSAT). Note that small discrepancies in p_{idle} were already observed in Section III for “Uniform Quant.” T_{off} . These small errors propagate to the WiFi CSAT throughput (via c_1) and to the LTE throughput (via c_2) but become negligible as T_{on} and T_{off} become respectively larger. For the case of BEB and variable packet lengths, relative errors are no higher than 15% and only significant for $n = 9$ when the probability of longer collisions due to different packet transmission durations increases.

It can be seen that the WiFi throughput is essentially the same when using either CSAT and LBE for all configurations, partially resolving current controversy on the ability of CSAT and LBE to provide fairness to WiFi. In contrast, however, the LTE throughput varies depending on the coexistence mechanism used and the network conditions. For example, we can observe a considerable decrease in throughput when CSAT is used for $T_{\text{on}} = 10$ ms and larger WiFi packet sizes (see Figs. 4a-c). Further inspection reveals that the reason for this is the increased collision probability between LTE and WiFi transmissions when using CSAT compared to LBE.

⁵Experimental validation of the simulator used is presented in the Appendix.

⁶For a discussion on these assumptions refer to Section VII.

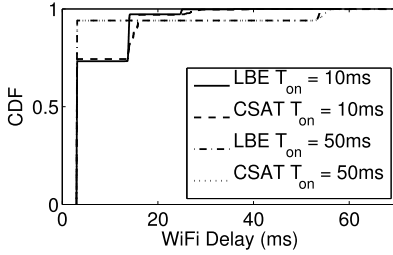


Fig. 5. CDF of delay for WiFi nodes with $n = 1$, $n_{\text{agg}} = 60$ packets. Results obtained from 100 simulation runs with 50 s time horizon.

Collisions between LTE and WiFi are part of the cost of heterogeneity discussed in Section III-B, and in a proportional fair rate allocation are accounted for in the LTE channel airtime (by Theorem 1). This cost of heterogeneity can be reduced by increasing the duration T_{on} of each LTE transmission. For example, we can observe in Figs. 4d-f that both the CSAT and LBE schemes provide similar LTE throughput for $T_{\text{on}} = 50$ ms. However, the duration of LTE transmissions will tend to increase the delay experienced by WiFi and we consider this in more detail next.

2) *Throughput vs Delay*: Although increasing the duration of the LTE transmissions improves LTE throughput and reduces the cost of heterogeneity, it may also increase the delay experienced by WiFi transmissions when WiFi stations defer their transmissions while LTE transmissions are ongoing. We investigate the distribution of the MAC access delay of WiFi packets when LTE uses CSAT and LBE in order to assess the trade-off between LTE throughput and WiFi delay.

Fig. 5 shows the measured CDF of the WiFi MAC access delay when $n = 1$, $n_{\text{agg}} = 60$ packets and for $T_{\text{on}} = 10$ ms and $T_{\text{on}} = 50$ ms. It can be seen that for a given value of T_{on} , the distribution of the WiFi delay is similar for both CSAT and LBE. We can also see that increasing T_{on} causes longer delays for a fraction of the WiFi packets (namely, those whose transmission has been deferred while an LTE transmission is in progress). Note that increasing T_{on} while maintaining the proportional fair configuration also causes the LTE network to access the channel less often, that is T_{off} also increases correspondingly. The consequence of this is that a higher percentage of the WiFi packets can access the channel during T_{off} , experiencing short delays and so the *mean* WiFi packet delay actually falls as the LTE T_{on} increases. However, a fraction of WiFi packets experience long delays. For example, for $T_{\text{on}} = 10$ ms it can be seen from Fig. 5 that around 73% of the WiFi transmissions observe short delays, while for $T_{\text{on}} = 50$ ms, this percentage increases to $\sim 94\%$.

V. NETWORKS WITH A MIXTURE OF UNSATURATED AND SATURATED STATIONS

Fair coexistence is only relevant when one or more stations are saturated (are persistently backlogged and so always have a packet to send). Otherwise, all stations can serve all of their offered load and there is no need to consider fairness in resource sharing. In this section we extend consideration to situations where some CSMA/CA stations may be unsaturated, i.e. that have a buffer but are not persistently backlogged.

A. Utility Fair Optimisation

When CSMA/CA stations are saturated their transmission attempt probability τ_j is fixed. However, for unsaturated stations τ_j depends upon both the offered load and the network load (since the latter affects the mean MAC slot duration) as well as any buffer dynamics. To extend our analysis to consider the case of unsaturated CSMA/CA stations we therefore make the following simplifying assumptions:

1. *Small buffers*. If the buffers are long, then during a T_{on} period unsaturated CSMA/CA stations may accumulate packets that are then transmitted during the T_{off} period. That is, the transmission activity of the scheduled network can therefore affect the transmission probability of the unsaturated CSMA/CA stations during the T_{off} period as it has an effect on buffer dynamics. In order to avoid consideration of these buffer dynamics, which make the analysis much less tractable, we assume small buffers and neglect this effect. The throughput model in Section IV-A then applies unchanged.

2. *p_e constant at rate region boundary*. As in [30] we assume that at the boundary region the probability of a CSMA/CA MAC slot being empty can be considered constant i.e. $p_e = \bar{p}_e$ where \bar{p}_e is a fixed parameter. As noted in [30], this approximation is generally accurate and involves little loss.

With these assumptions we have,

$$\tilde{s}_{\text{csma},j} = \tilde{x}_j + \log \bar{p}_e + \log D_j - (\sigma \bar{p}_e + \Delta(1 - \bar{p}_e)) + \tilde{z} - \log(T_{\text{on}} + c_1 + e^{\tilde{z}}), \quad j = 1, \dots, n \quad (14)$$

where we have performed the change of variable $x_j = \tau_j / (1 - \tau_j)$ resulting in $p_{\text{succ},j} = x_j \bar{p}_e$, and $\tilde{x} := \log x$.

Rearranging the terms and putting the constraints in standard form, the proportional fair optimisation problem is:

$$\max_{\substack{\tilde{s}_{\text{csma},j}, \tilde{s}_{\text{txA}}, \\ \tilde{z}, \tilde{x}_j}} \tilde{s}_{\text{txA}} + \sum_{j=1}^n \tilde{s}_{\text{csma},j} \quad (15)$$

$$s.t. \quad \tilde{s}_{\text{txA}} - \log q + \log(T_{\text{on}} + c_1 + e^{\tilde{z}}) \leq 0, \quad (15)$$

$$\tilde{s}_{\text{csma},j} - (\tilde{x}_j + \log \bar{p}_e + \log D_j - c_3(\tilde{z}) + \tilde{z}) \leq 0, \quad (16)$$

$$\tilde{s}_{\text{csma},j} - \tilde{\tilde{s}}_{\text{csma},j} \leq 0, \quad j = 1, \dots, n \quad (17)$$

$$\log \sum_{j=1}^n (1 + e^{\tilde{x}_j}) \leq -\log \bar{p}_e, \quad (18)$$

where $c_3(\tilde{z}) := \log(\bar{p}_e(\sigma - \Delta) + \Delta) + \log(T_{\text{on}} + c_1 + e^{\tilde{z}})$ and constraint (17) takes into account that the transmission probability is bounded by the offered load at a station (denoted by $\tilde{s}_{\text{csma},j}$). Note that the CSMA/CA transmission attempt probabilities are now included as decision variables x_j , $j = 1, \dots, n$ rather than being taken as constant as in the saturated case considered previously.

B. Proportional Fair Allocation

We next show that at an optimum, constraint (18) is tight.

Lemma 1: Suppose $C \subset \{1, \dots, n\}$, the set of CSMA/CA stations for which the optimal rate $\tilde{s}_{\text{csma},j}^ < \tilde{\tilde{s}}_{\text{csma},j}$ is not*

empty. Then at an optimum $\log \sum_{j=1}^n (1 + e^{\tilde{x}_j^*}) = -\log \bar{p}_e$ i.e. $\frac{1}{\prod_{j=1}^n (1 + e^{\tilde{x}_j^*})} = \bar{p}_e$.

Proof: We proceed by contradiction. Suppose that \tilde{x}_j^* , $j = 1, \dots, n$ is an optimum and $\log \sum_{j=1}^n (1 + e^{\tilde{x}_j^*}) < -\log \bar{p}_e$. We can thus increase \tilde{x}_j^* for one or more stations without violating constraint (18). Since for at least one station constraint (17) is loose, by increasing \tilde{x}_j^* for that station then constraint (16) becomes loose (since increasing \tilde{x}_j^* increases the RHS of (16) without changing the LHS). Constraints (18) and (16) are now both loose and so we can increase $\tilde{s}_{\text{csma},j}$. But increasing $\tilde{s}_{\text{csma},j}$ improves the objective of the optimisation, contradicting the assumption that we are at an optimum. ■

With Lemma 1 in hand we can now state the proportional fair rate allocation:

Theorem 2: The proportional fair rate allocation assigns the following fraction of airtime to the CSMA/CA transmitters:

$$\frac{\bar{T}_{\text{off}}^* - c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \frac{|C| + \sum_{j \notin C} \lambda_j^*}{1 + |C| + \sum_{j \notin C} \lambda_j^*}, \quad (19)$$

where C is the set of saturated CSMA/CA stations (assumed to be non-empty) and λ_j^* is the fraction of airtime used by CSMA/CA station j relative to that used by a saturated CSMA/CA station (so $\lambda_j^* = 1$ for saturated stations and $\lambda_j^* < 1$ for unsaturated stations).

Proof: The optimisation is jointly convex in the decision variables and the Lagrangian is,

$$\begin{aligned} L = & -\tilde{s}_{\text{txA}} - \sum_{j=1}^n \tilde{s}_{\text{csma},j} + \theta(\tilde{s}_{\text{txA}} - \log q + \log(T_{\text{on}} + c_1 + e^{\tilde{z}})) \\ & + \sum_{j=1}^n \lambda_j (\tilde{s}_{\text{csma},j} - (\tilde{x}_j + \log \bar{p}_e + \log D_j - c_3(\tilde{z}) + \tilde{z})) \\ & + \sum_{j=1}^n \mu_j (\tilde{s}_{\text{csma},j} - \tilde{s}_{\text{csma},j}) + \gamma (\log \sum_{j=1}^n (1 + e^{\tilde{x}_j}) + \log \bar{p}_e). \end{aligned}$$

The main KKT conditions are:

$$\begin{aligned} -1 + \theta^* &= 0, \quad -1 + \mu_j^* + \lambda_j^* = 0, \quad j = 1, \dots, n \\ (\theta^* + \sum_{j=1}^n \lambda_j^*) \frac{e^{\tilde{z}^*}}{T_{\text{on}} + c_1 + e^{\tilde{z}^*}} - \sum_{j=1}^n \lambda_j^* &= 0, \\ -\lambda_j^* + \gamma^* \frac{e^{\tilde{x}_j^*}}{\sum_{j=1}^n (1 + e^{\tilde{x}_j^*})} &= 0. \end{aligned}$$

Therefore at an optimum we have $\theta^* = 1$ and $\mu_j^* = 1 - \lambda_j^*$. Letting $C \subset \{1, \dots, n\}$ be the set of CSMA/CA stations for which the optimum rate $\tilde{s}_{\text{csma},j}^* < \tilde{s}_{\text{csma},j}$ (the set of saturated stations), then by complementary slackness we have $\mu_j^* = 0$, $j \in C$ and so $\lambda_j^* = 1$, $j \in C$. Combining the above with the KKT condition for \tilde{z} we have that at an optimum,

$$\frac{e^{\tilde{z}^*}}{T_{\text{on}} + c_1 + e^{\tilde{z}^*}} = \frac{\bar{T}_{\text{off}}^* - c_1}{T_{\text{on}} + \bar{T}_{\text{off}}^*} = \frac{|C| + \sum_{j \notin C} \lambda_j^*}{1 + |C| + \sum_{j \notin C} \lambda_j^*},$$

$$\text{where } \lambda_j^* = \gamma^* \frac{e^{\tilde{x}_j^*}}{\sum_{j=1}^n (1 + e^{\tilde{x}_j^*})} = \gamma^* \frac{x_j^*}{\sum_{j=1}^n (1 + x_j^*)}.$$

It remains to obtain λ_j^* for $j \notin C$ (for the set of unsaturated stations). We proceed by noting that the airtime used by CSMA/CA station j for successful transmissions is given by

$$T_{\text{csma},j} = \frac{\frac{\tau_j}{1-\tau_j} p_e \Delta}{\sigma p_e + \Delta(1-p_e)} \frac{z}{T_{\text{on}} + c_1 + z}, \quad (20)$$

where $p_e := \prod_{k=1}^n (1 - \tau_k) = \frac{1}{\prod_{k=1}^n (1 + e^{\tilde{x}_k})}$ is the idle probability. By Lemma 1 at an optimum

$$T_{\text{csma},j}^* = x_j^* \bar{p}_e \frac{\Delta}{c_4} \frac{z^*}{T_{\text{on}} + c_1 + z^*}, \quad (21)$$

with $c_4 = (\bar{p}_e(\sigma - \Delta) + \Delta)$. From the KKT conditions it follows that $\lambda_j^* = x_j^* \gamma^* \bar{p}_e$. Hence,

$$T_{\text{csma},j}^* = \lambda_j^* \frac{\Delta}{\gamma^* c_4} \frac{z^*}{T_{\text{on}} + c_1 + z^*}. \quad (22)$$

For a station $j \in C$ we know that $\lambda_j^* = 1$ and so at an optimum $T_{\text{csma},j}^* = T_{\text{csma},C}^* := \frac{\Delta}{\gamma^* c_4} \frac{z^*}{T_{\text{on}} + c_1 + z^*}$. Observe that the optimal airtime $T_{\text{csma},j}^*$ has the same value for all $j \in C$ since γ does not depend on j i.e. all stations unconstrained by offered load are allocated the same success airtime. For the stations $j \notin C$ from the above analysis we have $\lambda_j^* = \frac{T_{\text{csma},j}^*}{T_{\text{csma},C}^*} < 1$ while for stations $j \in C$ $\lambda_j^* = \frac{T_{\text{csma},j}^*}{T_{\text{csma},C}^*} = 1$. That is, $\lambda_j^* = \frac{T_{\text{csma},j}^*}{T_{\text{csma},C}^*}$ for all stations, and this is just the fraction of airtime used by CSMA/CA station j relative to that used by a CSMA/CA station unconstrained by offered load. ■

C. Discussion

It can be seen that Theorem 2 reduces to Theorem 1 when all of the CSMA/CA stations are saturated. Further, Theorem 2 has an elegant channel time interpretation. Namely, it states that the airtime allocated to the scheduled network is the same as the total channel time effectively used by the CSMA/CA network divided among an *equivalent* number of stations. This *equivalent* number of CSMA/CA stations is computed based on the proportion of success airtime of an unsaturated station compared to a saturated one.

D. Example: Unlicensed LTE and 802.11

We revisit here again the example in Section IV-D to illustrate the results obtained in the analysis above when there is a set of unsaturated WiFi stations. The same parameters as in the former example are used except that here in order to avoid consideration of the impact of the buffer dynamics, we assume no aggregation. To compute \bar{p}_e as well as τ_j , $j = 1, \dots, n$ for a given WiFi configuration, we have used a standard unsaturated model [31], considering that the buffer size is now limited to 5 packets of 1500 bytes.

Fig. 6 shows for CSAT the proportion of allocated channel time and successful airtime for the cases where: *i*) $n = 3$, $|C| = 2$ and, *ii*) $n = 9$, $|C| = 5$. In the former, the unsaturated offered load equals 10 Mbps while in the latter it is set to 3 Mbps. In the figure, the *Assigned Channel Time* proportion is equal to $T_{\text{on}} / (T_{\text{on}} + \bar{T}_{\text{off}})$ for LTE. In the case of WiFi, we define the *Assigned Channel Time* to be $(1 - \bar{T}_{\text{off}}) / n_{\text{eq}}$ for a saturated WiFi station and $\lambda_j^* (1 - \bar{T}_{\text{off}}) / n_{\text{eq}}$ for an unsaturated

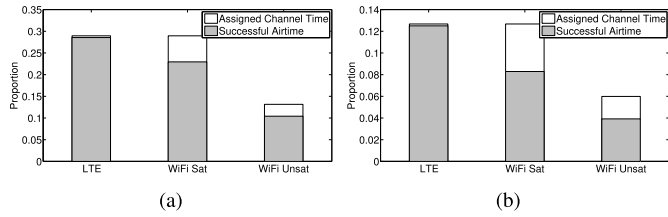


Fig. 6. Resulting proportional fair airtimes for different n and C . (a) $n = 3$, $|C| = 2$. (b) $n = 9$, $|C| = 5$.

one, which $n_{eq} = |C| + \sum_{j \notin C} \lambda_j^*$. This allows us to evaluate the channel time *allocated* to a station, although that includes empty periods and collision airtimes for WiFi, which are in fact shared among all WiFi stations. The successful airtime is also depicted in Fig. 6 and it corresponds to $(T_{on} - c1) / (T_{on} + \bar{T}_{off})$ for LTE and to (20) for WiFi.

We can see in Fig. 6 how the solution of the proportional fair optimisation problem assigns equal channel times to LTE and to a saturated WiFi station. Fig. 6 also illustrates the inefficiency of the WiFi channel access described in Section IV-C, and how in the presence of unsaturated WiFi stations this cost is not shared equally among all stations but varies proportionally to the offered load.

VI. IMPERFECT INTER-TECHNOLOGY TRANSMISSION DETECTION

Our focus is on random access transmitters which use carrier sensing to define MAC slots. In the foregoing analysis we have assumed that the random access transmitters can use their carrier sensing ability to also detect scheduled transmissions in fixed time slots and so defer their channel attempts while scheduled transmissions take place. In this section we now relax this assumption and consider imperfect sensing of scheduled transmissions by the random access transmitters.⁷

To help motivate this analysis we begin by giving a brief overview of the carrier sensing used by 802.11 transmitters and then present experimental measurements evaluating the effectiveness of this carrier sensing at detecting LTE transmissions in the unlicensed band. Use of experimental measurements rather than simulations is important since not only is signal propagation indoors complex but also physical carrier sensing functionality is typically hardware-dependent.

A. Transmission Detection in 802.11

The 802.11 standard mandates two types of detection of ongoing transmissions, namely virtual carrier sensing and physical carrier sensing. Virtual carrier sensing operates at the MAC layer. Transmitters set a duration field in the MAC header and receivers set a Network Allocation Vector (NAV) timer accordingly to mark the channel as busy for the duration requested in the transmitted frame. Physical carrier sensing is carried out at the PHY layer and employs one or more of the following methods: (i) Energy Detection, which declares the

channel to be busy when the received energy rises above a specified threshold, (ii) Weak Carrier Sensing, which detects the presence of OFDM transmissions, and (iii) Preamble Reception, which decodes the duration of the subsequent transmission from the PLCP preamble.

For detection of non-802.11 transmissions it is primarily physical carrier sensing using Energy Detection that is relevant since virtual carrier sensing and Preamble Reception are both 802.11-specific and Weak Carrier Sensing may also use 802.11-specific OFDM features. In general, Energy Detection is the least sensitive form of carrier sensing as it makes use of energy measurements instead of decoded information and is therefore prone to false negatives unless the energy detection threshold is set sufficiently high.

B. Testbed Hardware and Software Setup

We constructed a small test-bed to assess the ability of WiFi devices to detect unlicensed-band LTE transmissions.

1) *LTE SDR Transmitter*: We used an Ettus USRP B210 board, connected via an USB 3.0 interface to a standard PC (Intel Core i7) running Linux Ubuntu Trusty, with the `uhd_driver` and version 1.0.0 of `srsLTE` [32], which is a free, open-source LTE library for implementing both an UE and an eNodeB. The USRP board acts as eNodeB, configured to use 100 physical resource blocks (i.e., 20 MHz bandwidth) in the 5 GHz band, MCS index 0 and implementing a periodic duty-cycle channel access scheme, similar to the proposed CSAT coexistence mechanism [33]. This was achieved by modifying the `srsLTE` example program `src/examples/pdsch_enodeb.c` to fix an active interval during which data is transmitted, followed by a silent period of random duration. The average total duration of the active plus silent periods is set equal to 100 ms, and by varying the mean duration of the silent period we change the *duty cycle* of the LTE link. The LTE transmission power is also varied.

2) *WiFi SDR Transmitter*: To provide a baseline comparison, in our experiments we also operate the USRP board as an IEEE 802.11a transceiver.⁸ We generate a similar *on-off* WiFi transmission pattern as the one used for the LTE transmissions, in the same frequency channel and using the 6 Mbps MCS (which is the closest 802.11-compliant modulation and coding scheme to that of the LTE transmissions). The *on-off* WiFi transmissions are generated by transmitting WiFi packets in bursts during the *on* periods (with no idle time between packets, i.e. no DIFS and no random backoff), while remaining silent during the random *off* periods.

3) *WiFi Receiver*: WiFi channel sensing is performed by a Soekris net6501-70 device equipped with an Atheros AR9390-based 802.11a card, running Linux Ubuntu (kernel 3.13) and the `ath9k` wireless driver. We take advantage of this driver's monitoring capabilities to obtain the status of the medium as detected by the wireless card. This is achieved by leveraging `ath9k`'s 32-bit register counters `AR_CCCNT`, `AR_RCCNT`, and `AR_RFCNT`, which count, respectively, the total number of cycles elapsed (with a

⁷We do not anticipate imperfect detection in the other direction (of random access transmissions by the scheduled stations) as in the context of unlicensed LTE, we expect LTE carrier sensing to be designed to detect WiFi reliably.

⁸See <https://github.com/bastibl/gr-ieee802-11>. Note that the only available 5GHz implementation is based on 802.11a, so we are restricted to this.

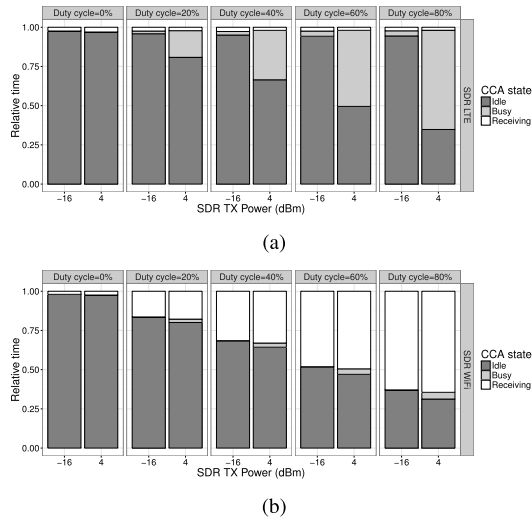


Fig. 7. WiFi Atheros CCA states. (a) SDR CSAT-based implementation. (b) SDR 802.11a implementation.

44 MHz resolution), the ones where the medium is marked as busy and the ones where there is an ongoing frame. With this data, we are able to measure the “CCA state” of the wireless medium (a similar approach is also used by RegMon [34]).

C. Experimental Measurements

Fig. 7(a) plots the measured “CCA state” at the WiFi receiver as the configuration (duty cycle and transmit power) of the LTE transmitter is varied. We start by considering the case with -16 dBm transmit power. We note that, given the small size of the testbed, for this configuration the signal quality was very good (we confirmed this using another Ettus board, configured as an unlicensed LTE UE). Nevertheless, it can be seen that the WiFi card consistently marks the channel as roughly 90% idle even when the LTE duty cycle is 80%. When the LTE transmit power is increased to 4 dBm, it can be seen that the situation changes and the WiFi card now marks the channel as becoming increasingly busy as the LTE duty cycle is increased. These measurements therefore show that WiFi carrier sensing fails at low LTE transmit powers.

For comparison Fig. 7(b) shows the corresponding measurements when the Ettus board is configured as a WiFi transmitter. It can be seen that the WiFi card correctly detects the medium as being occupied by 802.11 transmissions for both values of the transmit power, closely following the duty cycle.

These measurements demonstrate that the Energy Detection physical carrier sensing used by WiFi to detect LTE transmissions can be much less sensitive than the carrier sensing used by a WiFi station to detect WiFi transmissions.

D. Explicit Communication

The foregoing experimental measurements demonstrate the potential for much reduced sensitivity of random access carrier sensing when detecting scheduled transmissions rather than other random access transmissions,⁹ and therefore raise

⁹An extensive performance evaluation of unlicensed LTE/WiFi coexistence with imperfect detection is provided in [32].

concerns regarding imperfect sensing of scheduled transmissions. When physical carrier sensing of scheduled transmissions by random access transmitters is imperfect then interference (“collisions”) between scheduled and random access transmissions may increase substantially and so reduce network throughput and quality of service. For example, in the extreme case where random access transmitters cannot detect scheduled transmissions at all then scheduled throughput is likely to be much reduced.

One solution is to enable virtual carrier sensing via explicit communication between the scheduled and random access transmitters. This might be achieved, for example, by modifying scheduled transmitters to transmit a signal decodable by the random access network at the start of a T_{on} period to announce the duration of the transmission e.g. the scheduled transmitter might send a WiFi CTS-to-self packet (a 802.11 frame defined for backward compatibility). The use of explicit communication using the CTS-to-self in the context of unlicensed LTE and WiFi has been proposed in [33]. Upon successfully receiving this signal, the CSMA/CA transmitters will defer transmissions until the start of the next T_{off} interval. However, when such explicit communication is used for inter-network detection the explicit signaling is prone to loss. For example this may occur when the scheduled and random access transmitters begin transmission simultaneously at the start of a T_{on} period, leading to a collision. In this case, the concern is that random access transmitters will then be incapable of correctly decoding the signal sent by the scheduled transmitter.

E. Throughput Model with Explicit Communication

In this section we extend the throughput model in Section IV-A to include explicit communication between the scheduled and random access transmitters at the start of each T_{on} period, e.g. via the scheduled transmitter sending a CTS-to-self. The main difference from before is that we now need to take account of the fact that when a collision occurs at the start of a T_{on} period then the signal from the scheduled transmitter is lost and so the random access transmitters may continue transmitting during the T_{on} period rather than deferring to the scheduled transmission. For illustrative purposes and given that the conditions for correct detection are not yet fully understood, we consider the carrier sensing by the CSMA/CA network completely ineffective to detect LTE transmissions.

1) *CSMA/CA Throughput*: We first note that the CSMA/CA throughput during a T_{on} period is the same regardless of signalling from the scheduled network. Namely, either the CSMA/CA transmitters remain silent during the T_{on} period, and so no data is received, or the CSMA/CA transmissions during the T_{on} period collide with the scheduled transmissions and are lost, again with no data being received. However, when carrier sensing is imperfect then there may now be a partial collision at the end of the T_{on} period that extends beyond the scheduled transmission duration, affecting the value of $\mathbb{E}[T_{\text{off}}]$ (the mean time during which successful CSMA/CA transmissions are possible).

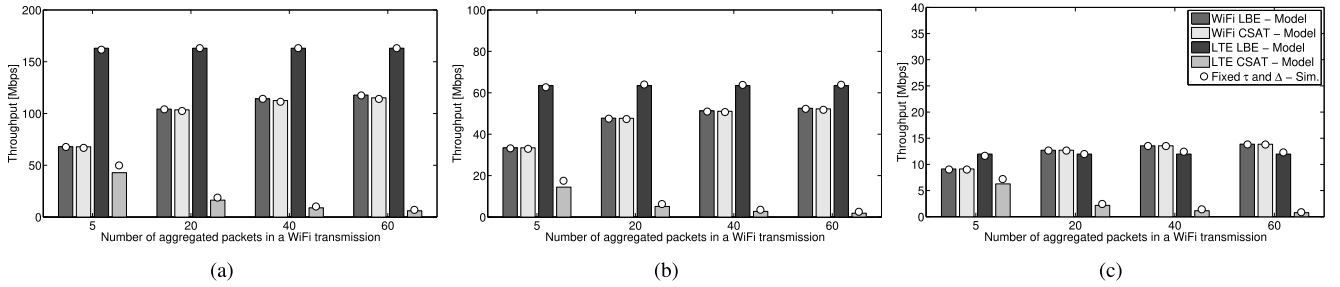


Fig. 8. Throughput with imperfect carrier sensing for different configurations of n and T_{on} while varying n_{agg} (effectively changing the packet size of WiFi transmissions). Simulation results are averages of 100 simulation runs with 50 s time horizon. (a) $n = 1, T_{\text{on}} = 50\text{ms}$. (b) $n = 3, T_{\text{on}} = 50\text{ms}$. (c) $n = 9, T_{\text{on}} = 50\text{ms}$.

Preemptive approach: Assuming that (i) on average the collisions at the end of the T_{on} period occur half-way through a CSMA/CA transmission, (ii) collisions at the start of the T_{on} period are independent of collisions at the end of T_{on} (which should hold when $T_{\text{on}} \gg \Delta$) and (iii) these collisions occur with probability $p_{\text{txA}} = \frac{(1-p_e)\Delta}{\mathbb{E}[M]}$, then:

$$\mathbb{E}[\hat{T}_{\text{off}}] = \bar{T}_{\text{off}} - \frac{\Delta}{2}p_{\text{txA}}(1 - p_{\text{txA}}) - \Delta p_{\text{txA}}^2. \quad (23)$$

Opportunistic approach: Similarly as for the *Preemptive* approach but considering that now partial collisions can only occur at the end of the T_{on} period, we have

$$\mathbb{E}[\hat{T}_{\text{off}}] = \bar{T}_{\text{off}} - \frac{\Delta}{2}(1 - p_e)p_{\text{txA}}, \quad (24)$$

where once again $p_{\text{txA}} = \frac{(1-p_e)\Delta}{\mathbb{E}[M]}$.

2) *Scheduled Network Throughput:* For simplicity we assume that the maximum idle space left between random access transmissions is smaller than the duration of a scheduled slot δ . Thus, when a collision occurs at the beginning of a T_{on} period then all of the scheduled frames in a slot are lost and we have the following.

Preemptive approach: We transmit successfully during T_{on} only in case of no collision with a CSMA/CA station:

$$s_{\text{txA}} = r \frac{T_{\text{on}}(1 - p_{\text{txA}})}{T_{\text{on}} + \bar{T}_{\text{off}}}. \quad (25)$$

Opportunistic approach: Only the duration $T_{\text{on}} - T_{\text{res}}$ adds to throughput as:

$$s_{\text{txA}} = r \frac{(T_{\text{on}} - T_{\text{res}})(1 - p_{\text{txA}})}{T_{\text{on}} + \bar{T}_{\text{off}}}, \quad (26)$$

with $p_{\text{txA}} = 1 - p_e$ as in Section IV-A. Note that when there is not a collision with a CSMA/CA node then $c_2 = T_{\text{res}}$.

F. Example: LTE and WiFi with Virtual Carrier Sensing

Using CTS-to-self as signalling approach, Fig. 8 shows the proportional fair result (as in Theorem 1) obtained using simulations and the analysis of throughput presented above. This can be compared with Fig. 4 but with the difference that WiFi now only defers to LTE when no LTE/WiFi collision occurs at the start of the T_{on} period, i.e. assuming that WiFi only defers to LTE upon correct reception of the CTS-to-self. It can be seen in Fig. 8, that the throughput of WiFi remains practically unchanged. However, the LTE throughput is

severely penalised for all configurations when using CSAT. The reason for this is the considerably higher collision probability of CSAT than LBE for the cases evaluated. Note also that LTE throughput is reduced compared to Fig. 4 for LBE when $n = 9$ due to the increase of the collision probability with the number of WiFi stations. Although the throughput in this case is not as reduced as with CSAT, the performance degradation is considerable. One way to alleviate this in LBE might be for the LTE to transmit before the DIFS to allow WiFi stations to decode the CTS-to-self, similarly to the approach described in [35], but this is outside the scope of the present paper.

VII. SCOPE AND PRACTICAL CONSIDERATIONS

In our analysis we have made a number of assumptions, many of which can be fairly readily relaxed. (i) *Loss-free channel:* Extension of our model to include channel losses is straightforward. Namely, by reducing the success probability with a packet loss probability. (ii) *Multiple Channels/Channel Bonding:* Both the scheduled and the random access networks may in general transmit across multiple channels. However, provided they occupy disjoint channels, we can solve the allocation problem separately for each set of channels using the model in Section IV-A. That is, although we focus on a single channel here, the generalisation to multiple channels is immediate. (iii) *Unsaturated Scheduled Network:* Extension of the analysis in Section V to the case in which the scheduled network is not saturated is straightforward if we ignore buffer dynamics and consider both T_{on} and T_{off} as random variables bounded by the offered load. (iv) *Multiple Scheduled Users:* The extension of this analysis to allow multiple users in the same scheduled network is straightforward for the *Preemptive* approach as the base station can coordinate transmissions by allocating specific slots to users. The *Opportunistic* approach is more complex in the uplink when LBE is required by all stations in the network as occurs in unlicensed LTE. However, current efforts concentrate on the downlink and assume the licensed interface is always active and used for uplink transmissions and control data [4].

We have also made a number of assumptions which are less easy to relax. (i) *Completely Overlapping Channels:* We have considered that the channel widths used by the coexisting networks completely overlap. The extension to smaller channel widths is not straightforward as it is not clear the level of interference that each technology will cause to one another when using heterogeneous and partially overlapping channel

widths. Refer to [14] for the case of unlicensed LTE and WiFi. (ii) *Capture*: Our model assumes that concurrent transmissions result in a collision and the inability of the receiver to decode the message. The main difficulty with including the capture effect in our analysis (where some receivers may successfully decode a colliding transmission) lies in specifying a suitable physical layer model and so we leave this for future work. (iii) *Hidden Terminals*: Perhaps the most significant omission from our analysis is hidden terminals. The basic difficulties here arise from the fact that hidden terminals can start transmitting even when a transmission by another station has already been in progress for some time and that the times hidden terminals attempt transmission are coupled to the dynamics of the transmissions they overhear. We therefore leave consideration of channel allocation with hidden terminals out of the scope of this work. It is perhaps also worth noting here that the prevalence of severe hidden terminals in real network deployments presently remains unclear. While it is relatively easy to construct hidden terminal configurations in the lab that exhibit gross unfairness, it may be that such configurations are less common in practice. (iv) *Fixed random-access slot transmission probability and equal successful and collision durations*: These assumptions are used in our analysis to ensure convexity of the optimization problem. The assumption on transmission durations can be relaxed using the approach in [36], taking account of the different transmission durations involved in a collision and transforming the convex problem via a change of variable. The fixed transmission probability assumption is harder to relax, but we have verified that our results show little sensitivity when this assumption is removed (and also when arbitrary transmission durations are used). (v) *Multiple Scheduled Networks*: The case of uncoordinated scheduled transmitters sharing the same unlicensed channel (as might be the case when they belong to different operators) is challenging as results depend greatly on the extent of the desynchronisation of their slot boundaries. It is worth noting though that current trends focus on assigning different unlicensed channels to neighbouring LTE networks.

Finally, we discuss the practical challenges when implementing our optimal configuration scheme in real hardware. Assuming the scheme runs on the scheduled transmitter, there are basically three challenges: (i) estimate the number of CSMA/CA stations (parameter n), (ii) classify them as saturated or unsaturated (set C of Theorem 2), and (iii) measure the average airtime lost due to partial slots (c_1 in Eq. 3). Concerning (i), approaches for estimating the number of contending stations are already known e.g. by passively sniffing the wireless activity [37] or through an explicit communication channel with the AP. For (ii), the classification of whether stations are saturated or not can also be achieved via sniffing: an indication of non-saturation is the number of slots between two consecutive transmission being larger than a backoff, while an indication of saturation are gaps in the L2 sequence numbers, due to queue drops. Finally, to estimate c_1 , note that, following the explanations after Eqs. 3 and 4, this parameter depends on the average time to transmit a frame (Δ), the relative proportion of empty slot times (p_e) and the average MAC slot length ($E[M]$), all of which can be easily estimated

again via sniffing and running the backoff procedure (similarly to, e.g., the implementation of *idle sense* [38]).

VIII. FINAL REMARKS

In this paper we address the coexistence of scheduled and random access transmitters in the same frequency channel. We show that there is an inherent cost due to the heterogeneity in channel access approaches. This cost is a per-transmission one and can thus be alleviated by increasing the duration of scheduled transmissions at the expense of increasing the variability of the delay for random access transmissions. We derive the joint proportional fair rate allocation and demonstrate that in this the heterogeneity cost is accounted for the channel airtime of the scheduled transmissions while the inefficiency of random access is accounted for in the channel airtime of the random access network. We extend this analysis to consider unsaturated random access stations as well as imperfect inter-technology detection. We illustrate the application of our analysis to the fair coexistence of LTE and WiFi. Importantly, we show that, when optimally configured, both CSAT and LBT/LBE, result in the same throughput to WiFi, providing significant new insight on the current controversy on their ability to provide fairness to WiFi. We also show that, in certain circumstances, the heterogeneity cost is higher for CSAT, and thus the resulting LTE throughput is lower when compared to use of LBT/LBE. We also show that in the case of imperfect inter-technology detection, the use of explicit communication is more problematic in CSAT due to the generally higher probability of loss compared to LBT/LBE.

APPENDIX EXPERIMENTAL VALIDATION

In the following, we present a validation of the simulator used in this work using experimental data for some simple scenarios. We use the same setup described in Section VI-B.1. Note that, since an LBT open-source LTE implementation is unavailable, we restrict our experimental comparison to CSAT. However, we remark that LBT is similar to the well-studied WiFi MAC protocol.

Fig. 9(a) shows the throughput of an LTE UE when both LTE eNB and WiFi Access Point transmission powers are equal to 12 dBm and 0dBm, respectively. Our SDR-based unlicensed LTE implementation is constrained to an in-band control channel which is transmitted in both on and off periods.¹⁰ Thus, by using low WiFi transmission powers, we guarantee that WiFi transmissions do not interfere with LTE's control channel, which is important to maintain both eNB and UE synchronized. The figure shows a good accuracy between the simulation results and the experimental data for different modulation indexes. We can observe slightly higher values when LTE uses modulation index 17 which are due to the fact that higher modulations are less robust to channel errors.¹¹

Fig. 9(b), on the other hand, shows the throughput observed in a WiFi link in the same setup as before but with WiFi transmission power equal to 17 dBm. The reason to use a different

¹⁰Note that current unlicensed LTE approaches consider to send these control channels through the licensed interface instead [4].

¹¹See Section VII for a discussion on extension to a lossy channel.

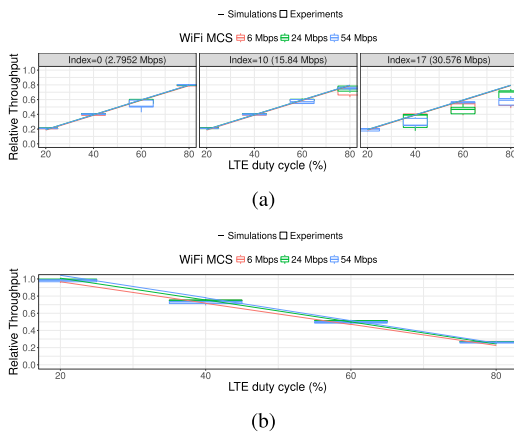


Fig. 9. Comparison of experimental and simulation data. (a) LTE throughput. (b) WiFi throughput.

value in this case is so we mitigate the interfering effects of the in-band LTE control channel during off cycles. As noted earlier, this is a limitation of our SDR-based implementation. Since, actual CSAT approaches suggest out-of-band control channels instead, this power setting helps us mimic the real case. In addition, we skip results for different LTE modulations because they do not affect WiFi throughput. As before, we observe a good match between simulations and experiments.

REFERENCES

- [1] D. Flore, "Chairman summary," presented at the 3GPP Workshop LTE Unlicensed Spectr., Jun. 2014.
- [2] M. I. Rahman, A. Behravan, H. Koorapaty, J. Sachs, and K. Balachandran, "License-exempt LTE systems for secondary spectrum usage: Scenarios and first assessment," in *Proc. IEEE Symp. New Frontiers Dyn. Spectr. Access Netw. (DySPAN)*, May 2011, pp. 349–358.
- [3] Qualcomm Research, "LTE in unlicensed spectrum: Harmonious coexistence with Wi-Fi," Qualcomm Technol., Inc., San Diego, CA, USA, White Paper, Jun. 2014.
- [4] C. Cano, D. López-Pérez, H. Claussen, and D. J. Leith, "Using LTE in unlicensed bands: Potential benefits and coexistence issues," *IEEE Commun. Mag.*, vol. 54, no. 12, pp. 116–123, Dec. 2016.
- [5] X. Zhang and K. G. Shin, "Enabling coexistence of heterogeneous wireless systems: Case for ZigBee and WiFi," in *Proc. ACM Int. Symp. Mobile Ad Hoc Netw. Comput. (MobiHoc)*, 2011, p. 6.
- [6] L. Berlemann, C. Hoymann, G. Hiertz, and B. Walke, "Unlicensed operation of IEEE 802.16: Coexistence with 802.11(A) in shared frequency bands," in *Proc. IEEE 17th Int. Symp. Pers., Indoor Mobile Radio Commun. (PIMRC)*, Sep. 2006, pp. 1–5.
- [7] *IEEE Draft Standard for Local and Metropolitan Area Networks. Part 15.4: Low-Rate Wireless Personal Area Networks (LR-WPANs)*, IEEE Standard 802.15.4e, Apr. 2015.
- [8] *Proposed TGah Draft Amendment*, IEEE Standard P802.11, Task Group AH, 2013.
- [9] M. R. Palattella *et al.*, "Internet of Things in the 5G era: Enablers, architecture, and business models," *IEEE J. Sel. Areas Commun.*, vol. 34, no. 3, pp. 510–527, Mar. 2016.
- [10] L. Tytgat, O. Yaron, S. Pollin, I. Moerman, and P. Demeester, "Avoiding collisions between IEEE 802.11 and IEEE 802.15.4 through coexistence aware clear channel assessment," *EURASIP J. Wireless Commun. Netw.*, vol. 2012, no. 1, p. 137, 2012.
- [11] J. Kim *et al.*, "Coexistence of WiFi and WiMAX systems based on PS-request protocols," *Sensors*, vol. 11, no. 10, pp. 9700–9716, 2011.
- [12] A. M. Cavalcante *et al.*, "Performance evaluation of LTE and Wi-Fi coexistence in unlicensed bands," in *Proc. IEEE Veh. Technol. Conf. (VTC Spring)*, Jun. 2013, pp. 1–6.
- [13] A. Babaei, J. Andreoli-Fang, and B. Hamzeh, "On the impact of LTE-U on Wi-Fi performance," in *Proc. IEEE 25th Annu. Int. Symp. Pers., Indoor, Mobile Radio Commun. (PIMRC)*, Sep. 2014, pp. 1621–1625.
- [14] Y. Jian, C.-F. Shih, B. Krishnaswamy, and R. Sivakumar, "Coexistence of Wi-Fi and LAA-LTE: Experimental evaluation, analysis and insights," in *Proc. IEEE Int. Conf. Commun. (ICCW)*, Jun. 2015, pp. 2325–2331.
- [15] *Study on Licensed-Assisted Access to Unlicensed Spectrum (Release 13)*, document 3GPP TR 36.889 v13.0.0, 3rd Generation Partnership Project, 2015.
- [16] Nokia Networks, "Nokia LTE for unlicensed spectrum," Nokia, Espoo, Finland, White Paper, 2014.
- [17] Qualcomm Inc., "Extending the benefits of LTE-A to unlicensed spectrum," Qualcomm, San Diego, CA, USA, White Paper, 2014.
- [18] Huawei, "U-LTE: Unlicensed spectrum utilization of LTE," Huawei, Shenzhen, China, White Paper, 2014.
- [19] Z. Ning, M. Saisai, X. Jing, Z. Bin, and Z. Wei, "Unlicensed spectrum usage method for cellular communication systems," in *Proc. Int. Conf. Wireless Commun., Netw. Mobile Comput. (WiCOM)*, 2012, pp. 1–6.
- [20] S. Hajmohammad and H. Elbiaze, "Unlicensed spectrum splitting between Femtocell and WiFi," in *Proc. IEEE Int. Conf. Commun. (ICC)*, Jun. 2013, pp. 1883–1888.
- [21] F. Liu, E. Bala, E. Erkip, M. C. Beluri, and R. Yang, "Small-cell traffic balancing over licensed and unlicensed bands," *IEEE Trans. Veh. Technol.*, vol. 64, no. 12, pp. 5850–5865, Dec. 2015.
- [22] C. Cano and D. J. Leith, "Coexistence of WiFi and LTE in unlicensed bands: A proportional fair allocation scheme," in *Proc. IEEE Int. Conf. Commun. Workshop (ICCW)*, Jun. 2015, pp. 2288–2293.
- [23] Z. Guan and T. Melodia, "CU-LTE: Spectrally-efficient and fair coexistence between LTE and Wi-Fi in unlicensed bands," in *Proc. IEEE Int. Conf. Comput. Commun. (INFOCOM)*, Apr. 2016, pp. 1–9.
- [24] C. Cano and D. J. Leith, "Unlicensed LTE/WiFi coexistence: Is LBT inherently fairer than CSAT?" in *Proc. IEEE Int. Conf. Commun. (ICC)*, May 2016, pp. 1–6.
- [25] F. Baccelli, S. Machiraju, D. Veitch, and J. C. Bolot, "The role of PASTA in network measurement," *ACM SIGCOMM Comput. Commun. Rev.*, vol. 36, no. 4, pp. 231–242, 2006.
- [26] *Wireless LAN Medium Access Control (MAC) and Physical Layer (PHY) Specifications. Amendment 4: Enhancements for Very High Throughput for Operation in Bands Below 6 GHz*, ANSI/IEEE Standard 802.11ac, 2013.
- [27] A. Checco and D. J. Leith, "Proportional fairness in 802.11 wireless LANs," *IEEE Commun. Lett.*, vol. 15, no. 8, pp. 807–809, Aug. 2011.
- [28] Y. Yang and T.-S. P. Yum, "Delay distributions of slotted ALOHA and CSMA," *IEEE Trans. Commun.*, vol. 51, no. 11, pp. 1846–1857, Nov. 2003.
- [29] A. Garcia-Saavedra, A. Banchs, P. Serrano, and J. Widmer, "Distributed opportunistic scheduling: A control theoretic approach," in *Proc. IEEE Int. Conf. Comput. Commun. (INFOCOM)*, Mar. 2012, pp. 540–548.
- [30] V. G. Subramanian and D. J. Leith, "Convexity conditions for 802.11 WLANs," *IEEE Trans. Inf. Theory*, to be published.
- [31] B. Bellalta, M. Oliver, M. Meo, and M. Guerrero, "A simple model of the IEEE 802.11 MAC protocol with heterogeneous traffic flows," in *Proc. IEEE Eurocon*, Nov. 2005, pp. 1830–1833.
- [32] I. Gomez-Miguel *et al.*, "srsLTE: An open-source platform for LTE evolution and experimentation," in *Proc. 10th ACM Int. Workshop Wireless Netw. Testbeds, Experim. Eval. Characterization (WiNTECH)*, 2016, pp. 25–32.
- [33] A. K. Sadek, T. Kadous, K. Tang, H. Lee, and M. Fan, "Extending LTE to unlicensed band—Merit and coexistence," in *Proc. IEEE Int. Conf. Commun. Workshop (ICCW)*, Jun. 2015, pp. 2344–2349.
- [34] T. Hühn, "A measurement-based joint power and rate controller for IEEE 802.11 networks," Ph.D. dissertation, Dept. Elect. Eng. Comput. Sci., Oxford Brookes Univ., Oxford, U.K., 2013.
- [35] V. Valls, A. Garcia-Saavedra, X. Costa, and D. J. Leith, "Maximizing LTE capacity in unlicensed bands (LTE-U/LAA) while fairly coexisting with 802.11 WLANs," *IEEE Commun. Lett.*, vol. 20, no. 6, pp. 1219–1222, Jun. 2016.
- [36] P. Patras, A. Garcia-Saavedra, D. Malone, and D. J. Leith, "Rigorous and practical proportional-fair allocation for multi-rate Wi-Fi," *Ad Hoc Netw.*, vol. 36, pp. 21–34, Jan. 2016. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S1570870515001262>
- [37] G. Bianchi and I. Tinnirello, "Kalman filter estimation of the number of competing terminals in an IEEE 802.11 network," in *Proc. 22nd Annu. Joint Conf. IEEE Comput. Commun. Soc. (IEEE INFOCOM)*, vol. 2, Mar./Apr. 2003, pp. 844–852.
- [38] Y. Grunenberger, M. Heusse, F. Rousseau, and A. Duda, "Experience with an implementation of the idle sense wireless access method," in *Proc. ACM CoNEXT Conf. (CoNEXT)*, New York, NY, USA, 2007, pp. 24:1–24:12. [Online]. Available: <http://doi.acm.org/10.1145/1364654.1364685>



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